

Exploratory Comparison of Human Rib Structural Behavior in Two Dynamic Loading Scenarios

Amanda M. Agnew, Akshara Sreedhar, John H. Bolte IV, Yun-Seok Kang

Abstract The objective of this study was to evaluate biomechanical response differences in human ribs subjected to simplified anterior-posterior (AP) dynamic loading versus AP loading combined with lateral (AP-L). Twelve bilateral pairs of 6th human ribs from an age-distributed sample (54 ± 17 years) were included in this study. One rib within each pair was selected to undergo 2D simplified AP loading to failure at 2 m/s. The other rib within the pair was tested in the same AP scenario, but with the added element of a rigid plate to constrain lateral displacement (AP-L). This set-up was intended to simply represent the combined AP and lateral loading the thorax would experience with a shoulder-belt pretensioner and a side airbag in a side impact. Results showed a significant response difference in time to fracture, displacement, peak force, and structural stiffness between AP only and AP-L tests. This work highlights the complexity of combined loading on human ribs that has not previously been investigated, and provides important evidence to explore variability in whole thoracic response and injury severities in various scenarios with different combinations of restraints in physical and simulated experiments.

Keywords Combined thoracic loading, frontal impact, rib fracture, side impact, thorax

I. INTRODUCTION

Post-mortem human subject (PMHS) testing has been accomplished in various test scenarios throughout recent history. Frontal hub impacts [1-3], bench top belt loading tests [4-8], and sled tests [9-14] have provided critical thoracic biomechanical response and injury risk data [15-16]. Lateral thoracic tests have been approached in a similar manner [17-19] utilizing hub impacts [20], airbag loading [21-22], and sled tests [23-26]. Oblique or offset testing was later explored to compare thoracic response and injuries to the more traditional data as it became more apparent that purely frontal or purely lateral impacts are not always realistic [27-31].

This progression of work was necessary in order to better understand thoracic response, injury mechanisms, and injury thresholds and has resulted in useful safety tools such as anthropomorphic test devices (ATDs) and computational human body models (HBMs). However, because of the necessarily simplistic approach in all experimental work to various degrees, the performance of ATDs and HBMs are generally optimized to be unidirectional. They are tested for biofidelity or validated, and equipped with instrumentation (i.e., ATDs) that is often restricted to one direction only, as they are meant to be used to evaluate the effects of frontal *or* side impacts, but rarely both simultaneously. As a result, some vehicle restraint systems are similarly optimized to be unidirectional; frontal airbags or side airbags deploy in frontal or side impacts, respectively. However, seatbelts are designed to couple vehicle occupants to their seat regardless of the crash direction.

Pretensioning belts hold the torso tightly in the seat from the shoulder retractor and/or the buckle, and will deploy in most crash modes, e.g., front, oblique, and side. Although it is accepted that tethering occupants into the seat increases their level of protection in a crash, it is still unclear whether a pretensioning belt may influence occupant injury risk in all crash modes. For instance, a near side impact crash would result in combined loading of the bony thorax whereby the pretensioning seatbelt would provide loading in an anterior-posterior (AP) direction while either door panel intrusion or a side airbag would provide lateral loading to the thorax on the struck side. Lateral thoracic deflection is an established injury criterion in side impacts [18][23][32], but the role of AP belt loading due to pretensioning remains unexplored in this context despite the realistic presence of a shoulder belt positioned on occupants in almost every real-world and simulated (experimental or computational) side impact crash scenario [33].

Most retrospective or experimental studies focus on the effects of either the restraints meant for protection

in frontal crashes, i.e., belt with load limiters, steering wheel airbag [34], or the restraints meant for protection in side crashes independently [35], but rarely are the combined effects of these restraints considered, with a few exceptions [36-37]. While investigating thoracic biomechanical responses in small female PMHS' in a realistic side impact scenario, Shurtz et al. [38] found significant variation in the mechanism and timing of rib fracture occurrence relative to the different restraint interactions in these PMHS by using non-censored strain gauge data. They suggested future work focus on specifically exploring the effects of combined loading to the thorax [38], so their complex findings in concert with the general lack of knowledge in this area served as the main motivation for the current study. Similarly, while a plethora of whole rib dynamic biomechanical response and failure data exist for frontal loading [39-41], and although scarce, some data also exist for lateral loading [42], no whole rib experimental studies exist quantifying structural response to both frontal and lateral loading combined. Therefore, the objective of the current study was to identify biomechanical response differences in human ribs subjected to simplified anterior-posterior (AP) loading versus anterior-posterior loading with a lateral constraint (AP-L), in order to provide foundational evidence to instigate further exploration of combined loading in a more complex test scenario.

II. METHODS

Sample

Whole, excised ribs were isolated from tissue donors to The Ohio State University Body Donation Program or Lifeline of Ohio and stored at -20°C in normal saline soaked gauze. Twelve bilateral pairs of 6th human ribs from an age-distributed sample (54 ± 17 years) were included in this study. Ribs were chosen from individuals across the adult age spectrum (30-76 years) and such that males and females of similar age were represented in order to reduce the potential of an age or sex bias in the sample (Table I).

TABLE I
DEMOGRAPHICS & TEST MATRIX FOR RIB PAIRS

Pair	Age (yrs)	Sex	Height (cm)	Weight (cm)	Loading Condition	Rib Side
1	30	M	185	90	AP	R
					AP-L	L
2	30	F	168	77	AP	L
					AP-L	R
3	42	M	174	76	AP	L
					AP-L	R
4	43	F	173	89	AP	L
					AP-L	R
5	48	M	170	53	AP	R
					AP-L	L
6	47	F	163	76	AP	R
					AP-L	L
7	57	M	188	61	AP	L
					AP-L	R
8	57	F	163	50	AP	L
					AP-L	R
9	70	M	174	81	AP	R
					AP-L	L
10	72	F	168	41	AP	R
					AP-L	L
11	76	M	175	93	AP	L
					AP-L	R
12	76	F	160	68	AP	L
					AP-L	R

Experimental Testing

Based on previous work establishing symmetry between sides, it was assumed that ribs of the same level (i.e., 6th ribs) within pairs would exhibit similar properties [43-44]. Therefore, individual ribs within bilateral pairs were utilized for direct comparisons between two different loading conditions (Table I). One rib within each pair was randomly selected to undergo 2D simplified anterior-posterior (AP) loading to failure at 2m/s as has previously been described in detail elsewhere [39]. Instrumentation included a six-axis load cell (Humanetics, CRABI neck, IF-954, Plymouth, MI, USA) to record forces behind the vertebral rib end and a displacement potentiometer (AMETEK, Rayelco P-20A, Inc. Berwyn, PA, USA) to measure global displacement in the primary loading direction (-X) connected to the moving plate driving the sternal (anterior) rib end posteriorly (Fig. 1). Uni-axial strain gauges (CEA-06-062UW-350, Vishay Micro-Measurement, Shelton, CT, USA) were applied at four locations along the longitudinal axis of the rib; 30% and 60% of total rib curve length (Cv.Le; measured from the vertebral end) on the pleural and cutaneous surfaces.

The opposite side rib within each pair was tested in the same AP scenario, but with the added element of a stationary rigid aluminum plate to constrain lateral (Y) displacement (AP-L) and an additional six-axis load cell (Humanetics, Hybrid III 3 year lumbar, 2944JFL, Plymouth, MI, USA) above the plate (Fig. 2). The initial position of the plate was adjusted so each rib apex was just barely touching the plate, thereby not allowing for any lateral displacement (Y), i.e., bending, to occur during the event. This set-up was intended to simply approximate the combined anterior-posterior and lateral loading the thorax would experience with both a shoulder-belt pretensioner and a side airbag in a near-side impact crash. Peak force in X and Y directions, X displacement, structural stiffness (linear portion of F_x-D curve), and total energy (area under F_x-D curve) were calculated from Load Cell 1 for direct comparison between both loading scenarios as outlined in [39]. Peak force in X and Y were also calculated from Load Cell 2. All force and displacement data were filtered using Channel Frequency Class (CFC) 180 [45]. Fracture locations were documented relative to the total Curve Length (Cv.Le) of each rib as a normalized distance from the vertebral rib end. Additionally, strain data were observed raw to identify time of failure.

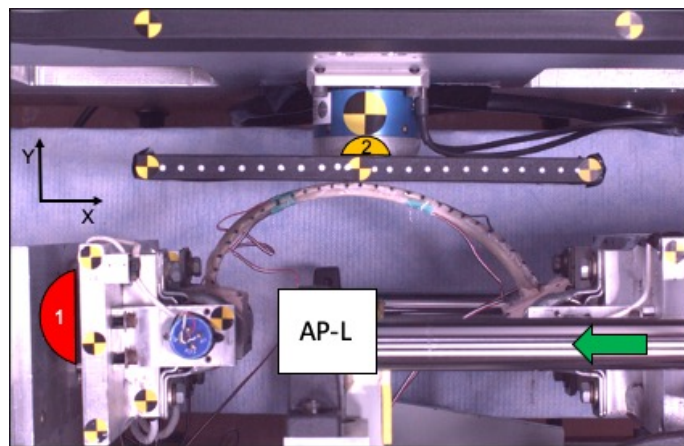
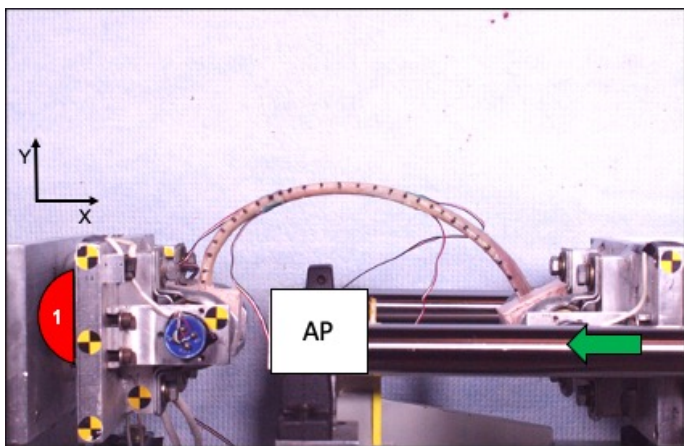


Fig. 1. Exemplar test set-up for AP loading condition (Left 6th rib from Pair 4) illustrating initial rib position (time zero) and Load Cell 1 posterior to the vertebral rib end.

Fig. 2. Exemplar test set-up for AP-L loading condition (Right 6th rib from Pair 4) illustrating initial rib position (time zero) and Load Cell 1 as well as Load Cell 2 above the added rigid plate.

Data Analysis

For comparison of all properties between AP and AP-L conditions, percent differences were calculated as:

$$\frac{AP\ value - APL\ value}{0.5 \times (AP\ value + APL\ value)} \times 100 \tag{1}$$

Mann-Whitney tests were utilized to assess differences in medians between loading conditions. Alpha level was set to 0.05 to establish statistical significance.

III. RESULTS

Structural properties comparisons between loading conditions are included in Table II, including results of Mann-Whitney tests for differences in medians (Minitab®18 Statistical Software) between AP and AP-L tests. It is important to recall these properties were calculated utilizing the load cell behind the vertebral rib end that was present for both conditions (Load Cell 1, Figs. 1-2), allowing for direct comparisons. All ribs tested in combined loading (AP-L) were not free to bend laterally as they naturally would and, therefore, fractured earlier than those loaded in AP ($p < 0.0001$). This resulted in significantly less displacement before failure in the AP-L tests ($p < 0.0001$). Peak force in the primary loading direction (X) was significantly greater in the AP-L loaded ribs compared to the AP only ($p = 0.004$). In combination with less displacement, the greater force magnitudes resulted in significantly greater structural stiffness ($p < 0.0001$) for ribs in the AP-L tests. Qualitatively, these differences are apparent in all twelve pairs of F_x -D responses shown in Figs. A1-A12. For the AP tests in which all the ribs remained unconstrained laterally, not surprisingly, the peak force in Y was very low, but with the addition of the lateral constraint the peak force in Y was significantly greater ($p < 0.0001$) with a median of 257N.

For the AP-L tests only, the load cell positioned above the rigid plate (Load Cell 2, Fig. 2) captured an average of 470N in the Y direction ($SD = 282N$, range=198-1268) and only 62N in the X direction ($SD = 36N$, range=30-160N), indicating the rigid plate did provide constraint as intended and that the friction as the rib slid posteriorly along the plate was minimal.

TABLE II
STRUCTURAL PROPERTY COMPARISONS FROM LOAD CELL 1

		Mean (SD)	Mean % Diff	Median	Diff Estimate	95% CI for Diff	p-value
Time of Fracture (ms)	AP	35.3 (11.6)		33.9			
	AP-L	17.4 (3.2)	68.1	17.1	15.8	10.8, 21.1	<0.0001
Displacement_x (%)	AP	22.8 (10.3)		20.1			
	AP-L	7.0 (3.1)	106.5	6.9	13.8	10.0, 17.9	<0.0001
Peak Force_x (N)	AP	110.2 (62.4)		102.0			
	AP-L	232.9 (184.7)	-71.5	188.2	-88.3	-137.9, -40.9	0.004
Peak Force_y (N)	AP	6.6 (3.5)		6.2			
	AP-L	283.8 (160.3)	-190.9	256.9	-247.1	-313.4, -172.6	<0.0001
Stiffness_x (N/mm)	AP	3.5 (2.6)		2.8			
	AP-L	37.2 (28.4)	-165.9	29.7	-26.5	-35.9, -19.0	<0.0001
Total Energy_x (N*mm)	AP	3387 (2384)		2369			
	AP-L	2278 (1487)	39.2*	2078	656	-627, 2635	0.237

*Mean % Diff of Total Energy included positive and negative values so should be interpreted with caution

Number and location of fractures were compared between AP and AP-L conditions (Table AI). As shown in Fig. 3, the range and median of fracture locations were not different between test conditions (Mann-Whitney, $p = 0.90$). However, with the presence of the lateral plate, it was observed that no fractures occurred in the middle portion of ribs that were pushed against the plate. The distribution is split such that fractures clustered on either end of these ribs. Because there were so few ribs that sustained three fractures (Table AI), differences between number of fractures sustained in AP vs AP-L tests could only be assessed for one and two fractures, for which no significant associations were found (Chi-square, $p = 0.46$).

not be directly comparable to the results of the current study, but the benefit of simulation is the same “ribs” were utilized so the results are surely due to loading changes and not rib variation [47]. Unfortunately, to our knowledge, no comparative experimental rib or thorax data for the AP-L loading scenario as explored here exist.

More research to explore the effects and the optimal timing of combined loading to the thorax is necessary. Both 2D loading conditions utilized in this study were oversimplified in order to ensure repeatability and allow for direct comparisons within rib pairs. Rib angle, costal cartilage, and other anatomical variations of the thorax were not accounted for. Furthermore, the boundary conditions were over constrained and did not represent realistic belt or airbag interactions, which could possibly result in unrealistic fracture locations. It is unknown why two groups of fracture locations emerged in the AP-L condition (Fig. 3) as no relationships between fracture location or any structural properties were found. It may be that the rapid pot rotations at the vertebral or sternal rib ends caused shearing to occur at either end (see Fig. A13 for a comparison of typical bending in the AP versus flattening and possible shear in the AP-L condition). This makes extrapolation of these findings to potential differential effects of loading conditions on whole thoracic response and injury in more realistic scenarios difficult. Further investigation of the effects of combined loading on intact PMHS thoraces is necessary as a next step in understanding this complex issue. This work, at the single rib level and whole thorax, can also be expanded to analyze strain modes to better understand differences in fracture mechanisms between AP and AP-L type loading.

Small sample size (n=12 pairs) is a limitation of this exploratory study, and further research is necessary. However, an attempt was made to age-match between sexes and to have a large range of ages of adults represented in order to incorporate human variability into the sample while also attempting to control for a possible bias of age or sex in results.

V. CONCLUSIONS

A large difference in human rib structural response between AP only and AP-L tests was observed, with a more severe outcome that occurred sooner when the lateral constraint was incorporated into the loading scenario. This may have implications for injury outcomes in more realistic PMHS tests and real-world motor vehicle crash scenarios in terms of timing of restraint system deployment. More work should be done in this area to further explore potential effects of combined loading to the thorax. This research highlights the complexity of combined loading on human ribs that has not been investigated using experimental methods previously and provides important evidence to explore variability in whole thoracic response and injury severities in various scenarios with different combinations of restraints in physical and simulated experiments.

VI. ACKNOWLEDGEMENTS

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VIII. APPENDIX

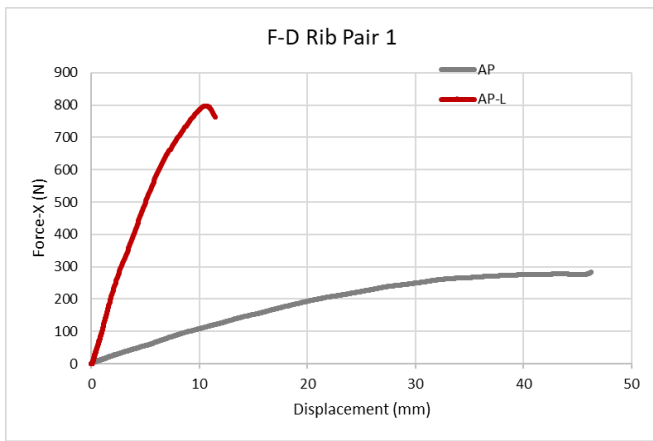


Fig. A1. Rib Pair 1 F_x-D Curves

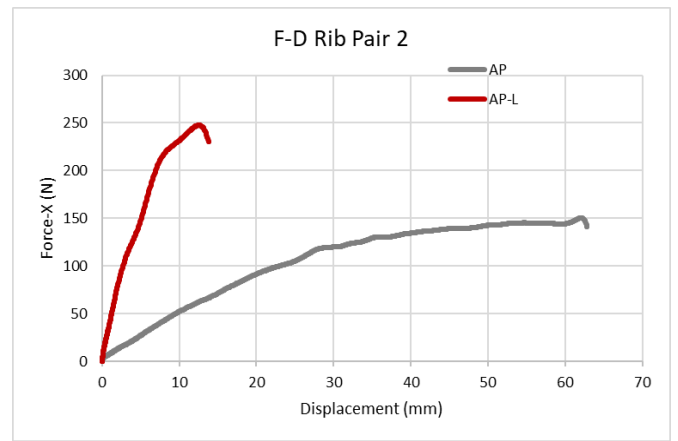


Fig. A2. Rib Pair 2 F_x-D Curves

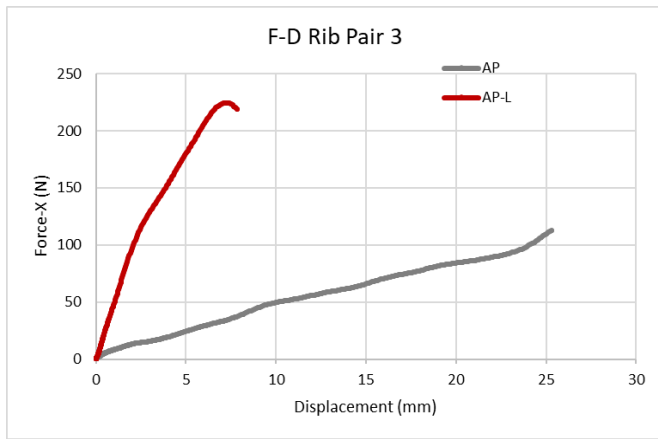


Fig. A3. Rib Pair 3 F_x-D Curves

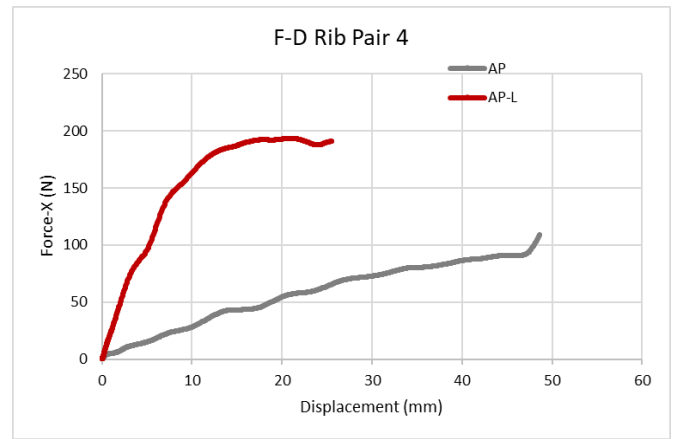


Fig. A4. Rib Pair 4 F_x-D Curves

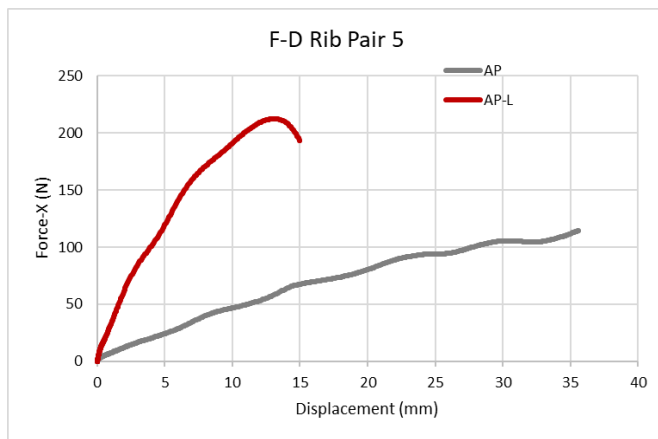


Fig. A5. Rib Pair 5 F_x-D Curves

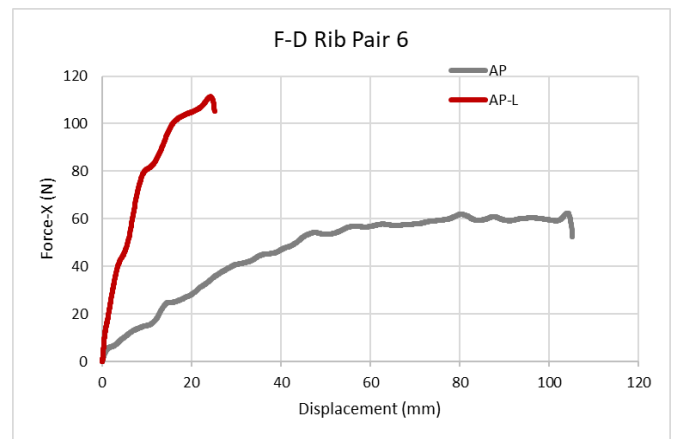


Fig. A6. Rib Pair 6 F_x-D Curves

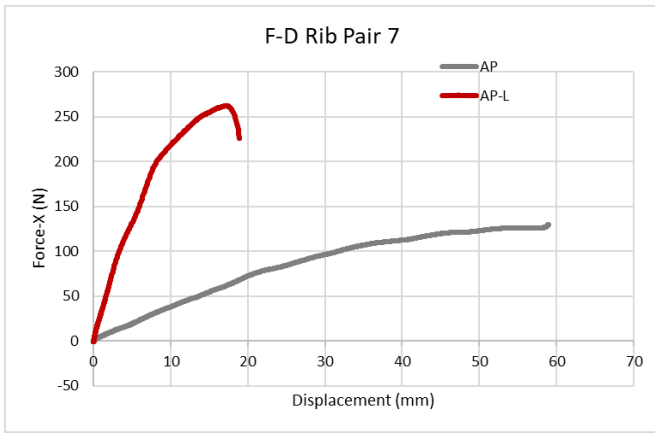


Fig. A7. Rib Pair 7 F_x-D Curves

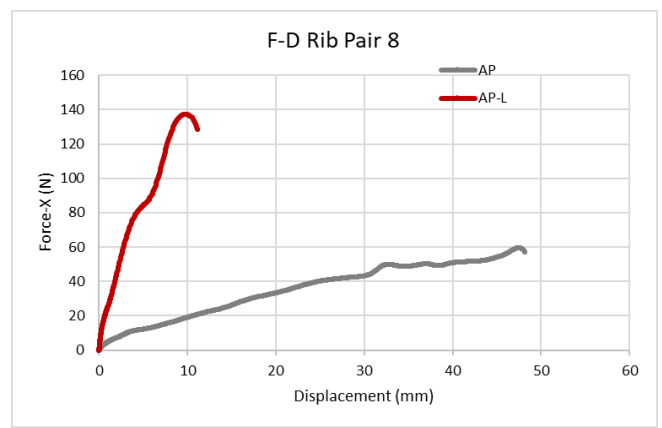


Fig. A8. Rib Pair 8 F_x-D Curves

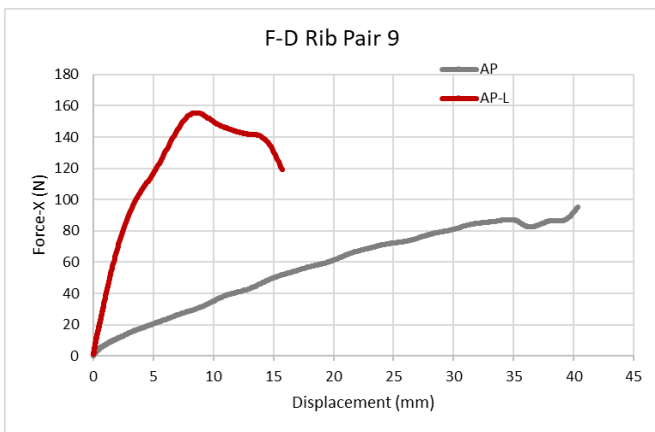


Fig. A9. Rib Pair 9 F_x-D Curves

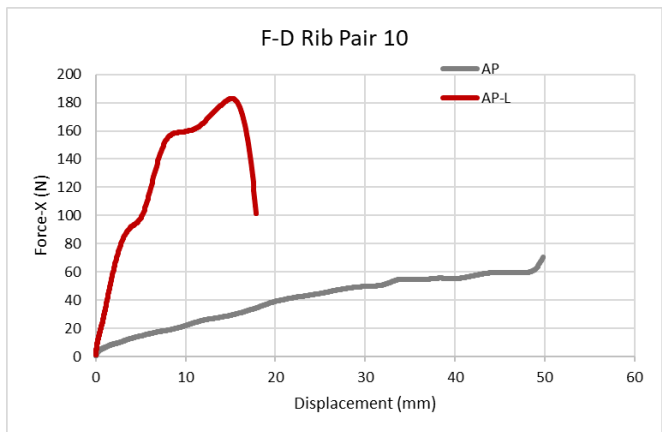


Fig. A10. Rib Pair 10 F_x-D Curves

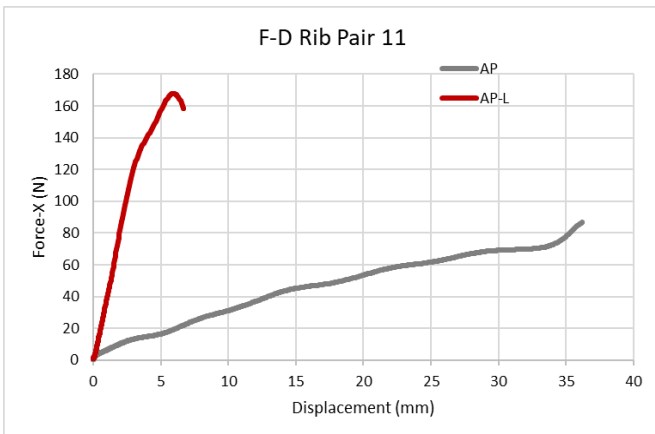


Fig. A11. Rib Pair 11 F_x-D Curves

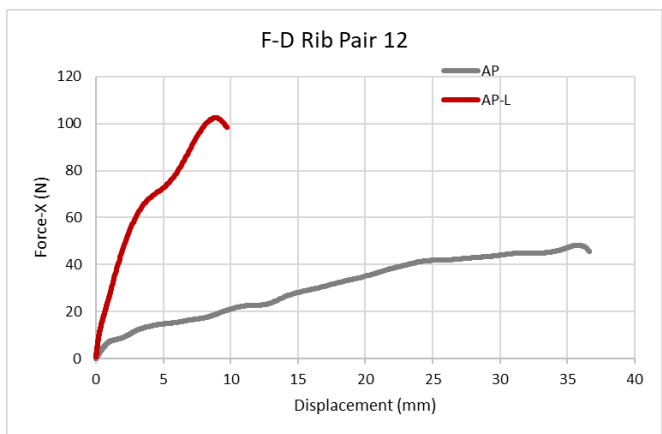


Fig. A12. Rib Pair 12 F_x-D Curves

TABLE AI
FRACTURE INFORMATION FOR RIB PAIRS

Pair	Loading Condition	Number of Fxs	Location of Fxs (%)
1	AP	1	90
	AP-L	1	66
2	AP	3	11, 47, 95
	AP-L	1	74
3	AP	1	65
	AP-L	1	71
4	AP	1	74
	AP-L	2	9, 93
5	AP	2	32, 86
	AP-L	2	14, 33
6	AP	2	39, 57
	AP-L	1	96
7	AP	1	84
	AP-L	1	6
8	AP	2	39, 83
	AP-L	1	89
9	AP	1	92
	AP-L	1	99
10	AP	1	74
	AP-L	1	18
11	AP	1	58
	AP-L	1	77
12	AP	3	39, 64, 81
	AP-L	1	70

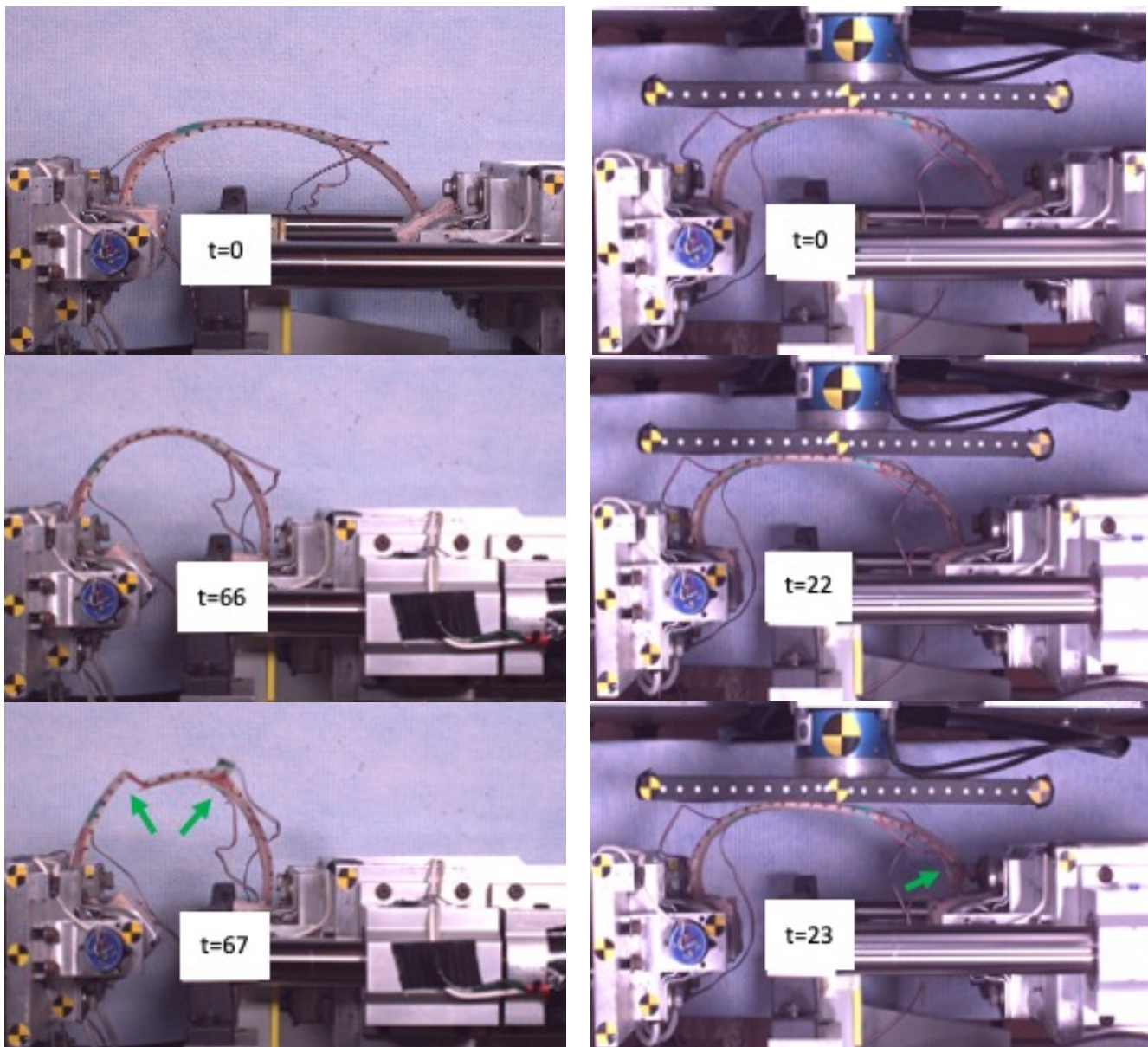


Fig. A13. Exemplar rib pair (Pair 6) comparing typical bending behavior in AP loading (left column) and a flattening effect from the rigid plate in AP-L (right column). Time (t) zero is in the top row, time just prior to fracture in the middle, and time of fracture in the bottom row. Times shown are in ms.